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# Modeling and Optimization of Performance and Cost of Serverless Applications

Changyuan Lin, Student Member, IEEE, Hamzeh Khazaei, Member, IEEE,

**Abstract**—Function-as-a-Service (FaaS) and serverless applications have proliferated significantly in recent years because of their high scalability, ease of resource management, and pay-as-you-go pricing model. However, cloud users are facing practical problems when they migrate their applications to the serverless pattern, which are the lack of analytical performance and billing model and the trade-off between limited budget and the desired quality of service of serverless applications. In this paper, we fill this gap by proposing and answering two research questions regarding the prediction and optimization of performance and cost of serverless applications. We propose a new construct to formally define a serverless application workflow, and then implement analytical models to predict the average end-to-end response time and the cost of the workflow. Consequently, we propose a heuristic algorithm named Probability Refined Critical Path Greedy algorithm (PRCP) with four greedy strategies to answer two fundamental optimization questions regarding the performance and the cost. We extensively evaluate the proposed models by conducting experimentation on AWS Lambda and Step Functions. Our analytical models can predict the performance and cost of serverless applications with more than 98% accuracy. The PRCP algorithms can achieve the optimal configurations of serverless applications with 97% accuracy on average.

Index Terms—Cloud Serverless Computing; Performance Modeling; Performance Optimization; Cost Modeling; Cost Optimization;

### **1** INTRODUCTION

Cloud computing has drawn extensive attention from both academia and industry over the past decade. A rapidly increasing number of applications and services are shifted to the cloud because of the high scalability, availability, payas-you-go billing model, and low overhead on infrastructure management [1], [2]. Meantime, many cloud service providers, such as Amazon Web Services (AWS), Google Cloud Platform (GCP), and Microsoft Azure, have emerged to offer diverse cloud services and infrastructures in the cloud computing market. With the increased popularity in containerization, service-oriented and event-driven architecture, there is also a growing trend in the paradigm of cloud computing shifting from Infrastructure-as-a-Service (IaaS) to Container-as-a-Service (CaaS) and Platform-as-a-Service (PaaS), and then to Function-as-a-Service (FaaS) [3]. Based on lightweight virtualization solutions, specifically containers, and container-orchestration systems, like Kubernetes, many cloud providers have launched their FaaS platforms, such as AWS Lambda, Google Cloud Functions, and Azure Functions.

With the development of FaaS platforms and evolution of the cloud computing paradigm, the serverless computing paradigm, in which the application is abstracted as a group of functions hosted on FaaS platforms orchestrated in a workflow has emerged. Serverless computing brings another revolution to cloud computing by rendering the

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management of underlying infrastructure unnecessary, as FaaS platforms take over all the operational responsibilities such as function deployment, resource management, scaling, and monitoring. Developers can mainly focus on the business logic of functions, thus expediting the application development. The small-granularity billing and scaling in FaaS platforms can also decrease the cost substantially [4], [5].

Despite the fact that serverless solution is cost-effective and eases the resource management, there are pain points hindering its wide adoption by potential users, including the lack of performance and cost model [6], [7], [8], and the trade-off analysis between the performance and cost of serverless applications [8], [9]. Performance and cost modeling and optimization are non-trivial and necessary steps towards guaranteeing the service level agreement (SLA) of serverless applications in an economic manner, which is basically finding an acceptable trade-off between performance and cost. The difficulties of such modeling and optimization problems lie in the following aspects:

- FaaS platforms introduce a new GB-second billing model depending on the memory size, function duration, and the number of invocations.
- 2) The workflow, which represents the orchestration of functions in serverless applications, can be very complex in terms of the number of functions, diverse structures, and the number of configuration combinations.
- 3) Classical methods used in the performance modeling of parallel computing and traditional software, such as Petri net and queuing theory, are not suitable for the serverless application because of its independently-operated, event-driven, closedsource, and infrastructure-agnostic architecture.

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Fig. 1. Overview of the proposed approach for modeling and optimization of performance and cost of serverless applications. The three boxes from left to right illustrate the input, performance and cost models and optimization algorithms, and the corresponding output. The cloud provider part can be replaced with any FaaS platforms. We use AWS for experimental evaluation in this work. The proposed approach can accomplish three types of tasks (depicted by three different colors): (i) Deploy user-provided function source code and payload to FaaS platform, invoke functions and query the execution log, and give the performance-memory curve of functions as shown in Figure 2 as the output. (ii) Take the workflow orchestration of the serverless application and memory configuration and performance (response time) of functions as inputs, process inputs using the performance and cost models, and give the application end-to-end response time and the average cost under the given configuration as the output. (iii) For user-defined performance and cost constraints of a workflow, leverage the proposed performance cost models and optimization algorithms with the performance-memory curve of functions, and give the satisfying memory configuration that achieves the best performance under a budget constraint or the minimum cost under a performance constraint as the output.

Such a significant gap leads us to the following research questions:

- **RQ1:** Can we obtain the end-to-end response time and cost of a serverless application when orchestration and configuration of the application are given?
- **RQ2**: Can we calculate the best performance under a given budget or the minimum cost for a desired performance for a serverless application?

To answer these research questions, we propose new analytical models and a greedy algorithm with four strategies to respectively model and optimize the performance and cost of serverless applications. The overview of the proposed approach is illustrated in Figure 1. We evaluated the model and algorithm using serverless applications deployed on AWS composed of three types of generic functions representing CPU, network, and disk intensive workloads, with parallels, branches, cycles, and self-loops in their workflows. As verified by the experimental evaluation, our analytical model can precisely give the end-to-end response time of serverless applications with over 98% accuracy, and estimate the average cost with an accuracy of over 99%, independent of the complexity of their workflows. The greedy algorithm can effectively and efficiently resolve two types of optimization problems specified in RQ2 with over 97% accuracy.

The main contributions of this paper are three-fold: (1) We propose a formal definition of the serverless application workflow to abstract sequence, parallelism, branch, cycle, and loop in the workflow and new features introduced by the serverless computing paradigm, such as the GB-second billing model and the orchestration of FaaS functions. (2) We propose, to the best of our knowledge, the first analytical models to accurately get the average end-to-end response time and cost of serverless applications with parallels, branches, cycles, and self-loops in their workflows. (3) We present a heuristic algorithm for optimizing performance and cost of serverless applications, which can give the optimal configurations of functions achieving the best performance for a given budget and the minimum cost for satisfying a given performance. All our algorithms, scripts, and experimental results are available in the artifact repository<sup>1</sup>.

The rest of the paper is organized as follows: Section 2 briefly introduces the background including FaaS, serverless application, and serverless workflow. Section 3 presents the construction of the serverless workflow and performance and cost models, namely answering the RQ1. In Section 4, we propose performance and cost optimization problems in RQ2 and the PRCP algorithm to answer them. Section 5, presents the experimental evaluation of the aforementioned models and algorithm. In Section 6, we survey the latest related literature in the areas of performance modeling, workflow scheduling, and serverless architecture. Section 7 discusses and concludes our work.

#### 2 BACKGROUND

In this section, we give a brief introduction to FaaS, serverless application, and serverless workflow.

#### 2.1 FaaS

In the Function as a Service (FaaS) paradigm, the function is a chunk of code that abstracts a part of an application implementing business logic. The notion of function in FaaS is similar to a function in functional programming or a method in object-oriented programming, responsible for handling one task required by the application statelessly. The source code of the function and its dependencies are packaged

1. https://github.com/pacslab/SLApp-PerfCost-MdlOpt



Fig. 2. The cost and performance with regard to the amount of allocated memory of a CPU-intensive function (hashing) deployed on AWS Lambda. The blue line is the performance-memory curve of the function.

together, and the function is running in an ephemeral isolated environment provided by lightweight virtualization solutions such as Docker containers, Unikernels [10], or even processes [11].

AWS launched a computing service called Lambda in 2014 [12], which could store, package, and deploy functions uploaded by users, handle events and requests of functions, monitor the resource usage, and autoscale function containers correspondingly. This was the first time that the function execution was offered as a cloud service, namely FaaS. Today, besides AWS Lambda, many FaaS platforms with similar functionalities are provided by public cloud service providers and open-source communities such as Google Cloud Functions, Azure Functions, and OpenFaaS.

As FaaS platforms take over operational responsibilities, besides uploading the source code of functions, users have limited control over resources on FaaS platforms. Taking AWS Lambda as an example, the amount of allocated memory during execution and the concurrency level are only options for tuning the performance of functions. The amount of allocated memory is between 128 MB and 3,008 MB in 64MB increments [13]. Previous researches have proven that computational power and network throughput are in proportion to the amount of allocated memory, and disk performance also increases with larger memory size due to less contention [14], [15]. By reserving and provisioning more instances to host functions, high concurrency level can decrease fluctuations in the function performance incurred by cold starts (container initialization provisioning delay if no warm instance is available) and reduce the number of throttles under very heavy request loads [16].

FaaS platforms also introduce a new GB-second billing model depending on the allocated memory size, function duration, and the number of invocations. For example, AWS Lambda charges \$0.000016667 for every GB-second and \$0.20 per 1M function invocations. The billed duration is the function duration rounded up to the nearest 100ms and metered at a granularity of 100ms [17]. Due to the rounding and billing granularity, the cost fluctuates erratically as the memory size changes, see our experiment results shown in Figure 2. The new billing model and such irregularities make the modeling and optimization problems non-trivial.



Fig. 3. Workflow of a serverless image classification application composed of seven FaaS functions. The two numbers on each function represent the response time and allocated memory, respectively. P and D are the transition probability function and the delay function.

#### 2.2 Serverless Application

The serverless application decouples its business logic into a group of serverless functions hosted on FaaS platforms and leverages necessary cloud services such as bucket storage, message queue, and pub/sub messaging service to build a stateless and event-driven software system [18], [19]. FaaS platforms and those cloud services shift most operational responsibilities to cloud service providers. Hence, the overhead of server management, monitoring, failover, and scaling is eliminated for serverless applications, like there are no servers to manage at all, namely serverless.

To complete the business logic of the application, interactions among decoupled functions are indispensable. In most cases, a coordinator is required to chain together components of the application, handle events among functions, and trigger functions in the correct order defined by the business logic. Typically, a message queue, a pub/sub messaging service, an event bus, or a workflow coordinator like AWS Step Functions Express Workflows act as such a coordinator [6], [18], [20]. Figure 3 illustrates an example of a serverless application composed of seven functions.

#### 2.3 Serverless Workflow

In general, the serverless workflow is the orchestration of functions in the serverless application to implement the entire business logic. AWS defines that the serverless workflow describes a process as a series of individual functions and coordinates them [21]. As shown in many examples of serverless applications deployed in the production environment, there can be four types of structures in the serverless workflow, including parallel, branch, cycle, and selfloop [22], [23], [24]. Many research works have proven that workflows based on the directed acyclic graph (DAG) and Petri net are effective for performance and cost modeling of systems in parallel, distributed, and scientific computing [25], [26], [27]. However, none of them are favorable for the serverless paradigm, as cycles and loops are not allowed in DAGs, and cause the state explosion problem without efficient solutions in Petri nets. The disadvantages of Petri nets also lie in its high complexity and limited support of nonfunctional requirements in cloud computing [28]. Hence, performance and cost modeling of serverless applications requires a loose and concise definition of the serverless

workflow, which adapts to new features of the serverless computing paradigm.

#### **3** Performance and Cost Modeling

In this section, we first construct the serverless workflow of a serverless application, and then propose two analytical models to predict the performance and cost, i.e., answering the RQ1.

#### 3.1 Definition of the serverless workflow

The serverless workflow of a serverless application  $G_s$  is defined as a weighted directed graph:

$$G_s = (V, E, P, D, RT, RTTP, M, NI, C)$$
(1)

where

- V is a finite set of |V| vertices  $\{f_1, f_2, ..., f_n\}$ , such that n = |V|, representing FaaS functions, integrated cloud services, or structural vertices;
- $E \subseteq V \times V$  is a finite set of directed edges. The directed edge from  $f_u \in V$  to  $f_v \in V$ , denoted as  $e_i = (f_u, f_v)$ , represents the interaction between vertex  $f_u$  and  $f_v$  defined by the business logic;
- $P: V \times V \rightarrow [0,1]$  is a transition probability function.  $P(f_u, f_v)$  identifies the probability of invoking  $f_v$  after finishing the execution of  $f_u$ . A transition probability of 0 represents the corresponding edge does not exist;
- $D: V \times V \rightarrow [0, +\infty)$  is a delay function.  $D(f_u, f_v)$  identifies the delay from  $f_u$  to  $f_v$  incurred by the interaction/coordination method;
- $RT: V \rightarrow [0, +\infty)$  is the response time of a function.  $RT(f_u)$  is the response time of function  $f_u$ ;
- $RTTP: V \rightarrow \wp ([0, +\infty) \times [0, 1])$  is a function representing all possible values of the response time and corresponding probability of interim B-nodes, which are defined in Section 3.3.1 to process branches.  $RTTP(f) \triangleq \emptyset$  for any *f* which is not a B-node;
- $M: V \to \mathbb{N}$  is a memory function.  $M(f_u)$  is the size of the allocated memory of function  $f_u$ ;
- *NI* : *V* → [0, +∞) is a function representing the average number of invocations of each function in *V*, per execution of the serverless workflow *G<sub>s</sub>*;
- $C: V \to [0, +\infty)$  is a cost function.  $C(f_u)$  is the cost per invocation of function  $f_u$ ;

Besides FaaS functions, vertices can also represent other cloud services, such as a MapReduce service or a database operation service. As those services are similar to functions in terms of the execution, we collectively call them functions for brevity. V can also contain several non-functional structural vertices that facilitate developing the workflow and do not incur any delay and cost, such as start node and end node. Typically, the execution of the serverless workflow starts with a particular function as a trigger, and then the following functions will be invoked to complete the business logic [29]. Therefore, we include a start node  $f_{str}$  and an end node  $f_{end}$  in V defining the entry point and the endpoint of the workflow, respectively. Figure 3 shows an example of a serverless workflow for image classification. Based on the definition of the serverless workflow, we define the following notations:

- 1) A simple path in the serverless workflow is a finite sequence of distinct vertices and edges  $s = f_1e_1f_2e_2...e_{n-1}f_n$  such that (i)  $f_i \in V$  for all integers  $1 \leq i \leq n$ , (ii)  $e_i \in E$  for all integers  $1 \leq i \leq n-1$ , and (iii)  $e_i = (f_i, f_{i+1})$  for all integers  $1 \leq i \leq n-1$ .
- 2) The transition probability of the simple path  $s = f_1 e_1 f_2 e_2 \dots e_{n-1} f_n$  is defined as Equation (2).

$$TPP(s) = \prod_{i=1}^{n-1} P(f_i, f_{i+1})$$
(2)

3) The delay (response time) of a simple path  $s = f_1 e_1 f_2 e_2 \dots e_{n-1} f_n$ , denoted as DLY(s), is defined as Equation (3), namely the sum of the response time of functions and the delay incurred by edges in this path. In particular, we use  $DLY^-(s)$  to denote the delay of a simple path without considering the response time of the first and last vertices in the simple path, defined as Equation (4).

$$DLY(s) = \sum_{i=1}^{n} RT(f_i) + \sum_{i=1}^{n-1} D(f_i, f_{i+1})$$
(3)

$$DLY^{-}(s) = \sum_{i=2}^{n-1} RT(f_i) + \sum_{i=1}^{n-1} D(f_i, f_{i+1}) \quad (4)$$

- ASP(f<sub>u</sub>, f<sub>v</sub>) denotes all simple paths between vertex f<sub>u</sub> and f<sub>v</sub>, which is the set of all possible simple paths in the workflow graph, starting from f<sub>u</sub> and ending at f<sub>v</sub>, with f<sub>u</sub> and f<sub>v</sub> included.
- 5) The shortest path length between two vertices  $f_u$  and  $f_v$ , denoted as  $SPL(f_u, f_v)$ , is specified as the length of the shortest simple path from  $f_u$  to  $f_v$ . The length of a simple path is the number of edges in it.
- SUB(f<sub>u</sub>, f<sub>v</sub>) denotes the subgraph between f<sub>u</sub> ∈ V and f<sub>v</sub> ∈ V, which is derived from G<sub>s</sub> by removing all vertices and edges not in any paths in ASP(f<sub>u</sub>, f<sub>v</sub>).
- out (f<sub>u</sub>) denotes the set of all edges starting from vertex f<sub>u</sub>, defined as the following.

$$out(f_u) = \{ e \in E : e = (f_u, f) \text{ for some } f \in V \}$$

For convenience, Table 1 includes the definitions of notations and parameters used in the performance and cost models as well as optimization algorithms.

#### 3.2 Structures in the serverless workflow

In this section, we define four types of structures in the serverless workflow, namely parallel, branch, cycle, and self-loop, as shown in Figure 4.

#### 3.2.1 Parallel

Let us consider all simple paths between vertices  $f_u \in V$ and  $f_v \in V$ . If there is more than one simple path whose transition probability is 1, we define the subgraph composed of all simple paths with the transition probability of 1 as a *parallel structure*.

TABLE 1 Definition of Notations used in models and algorithms

Notation	Definition	
C	the serverless workflow (eq. (1))	
$G_s$	$G_s = (V, E, P, D, RT, RTTP, M, NI, C)$	
f	a FaaS function, cloud service, or structural vertex	
$e = (f_u, f_v)$	a directed edge from $f_u$ to $f_v$	
s	a simple path	
TPP(s)	transition probability of a simple path $s$	
DLY(s)	elay of a simple path <i>s</i>	
$ASP(f_u, f_v)$	the set of all simple paths between $f_u$ and $f_v$	
$SPL(f_u, f_v)$	the shortest length of simple paths between $f_u$ and $f_v$	
$SUB(f_u, f_v)$	the subgraph between $f_u$ and $f_v$	
$out(f_u)$	the set of all edges starting from $f_u$	
ERT(G)	the end-to-end response time of the workflow $G$	
ø	power set	
ŧ	disjoint union	
$\Downarrow$	restriction of a function	
$\mapsto$	map an element in the function domain	
A	the cardinal number of a set	
$G_p$	a parallel structure	
$G_b$	a branch structure	
$G_c$	a cycle structure	
$G_l$	a self-loop structure	
$G_{pr}$	probabilistic DAG used in the performance model	
$G_{dl}$	de-looped graph (DAG) used in the cost model	
$G_{perf}$	the graph used in the performance model (eq. (5))	
$G_{cost}$	the graph used in the cost model (eq. (12))	
SRT(G)	the RT of a parallel/branch/cycle/self-loop	
EI(G)	the expected number of iterations of a cycle/self-loop	
DI(G)	the delay incurred by iterations of a cycle/self-loop	
$f_B$	a B-node used in procedures of processing branches	
$f_P$	a P-node used in procedures of processing parallels	
PGC	price per GB-second of FaaS functions	
PI	price per invocation of FaaS functions	
W(s)	weight of a simple path <i>s</i>	
BCR	Benefit-cost ratio	
TH	BCR threshold	
$\beta(f_u)$	the slope of the performance-memory curve of $f_u$	

Namely, we define the subgraph  $G_p = (V_p, E_p)$  as a parallel structure, such that  $|SP_p| > 1$ , where

$$V_{p} = \{f \in V : \text{f is in s for some s} \in SP_{p}\}$$
$$E_{p} = \{e \in E : e \text{ is in } s \text{ for some s} \in SP_{p}\}$$
$$SP_{p} = \{s \in ASP(f_{u}, f_{v}) : TPP(s) = 1\}$$

As the parallel shown in Figure 4, the vertices and edges of the parallel structure are depicted in blue color. There are two simple paths with the transition probability of 1 between  $f_1$  and  $f_4$ , namely  $f_1e_1f_2e_3f_4$  and  $f_1e_2f_3e_4f_4$ . Functions  $f_2$  and  $f_3$  are processed in parallel, indicating that  $f_1$  leverages interactions to invoke  $f_2$  and  $f_3$  at the same time after finishing its execution, and  $f_4$  starts execution only after both  $f_2$  and  $f_3$  are completed.

#### 3.2.2 Branch

Let us consider all simple paths between vertices  $f_u \in V$ and  $f_v \in V$ . If there is more than one simple path whose transition probability is less than 1, but can sum up to 1



Fig. 4. Four types of structures in the serverless workflow.

in total, we define the subgraph composed of those simple paths with the transition probability not equal to 1 as a *branch structure*.

Namely, we define the subgraph  $G_b = (V_b, E_b)$  as a branch structure, such that  $|SP_b| > 1$ , where

$$V_{b} = \{f \in V : \text{f is in s for some } s \in SP_{b}\}$$
$$E_{b} = \{e \in E : e \text{ is in } s \text{ for some } s \in SP_{b}\}$$
$$SP_{b} = \{s \in ASP(f_{u}, f_{v}) : TPP(s) \neq 1\}$$
$$\sum_{s \in SP_{b}} TPP(s) = 1$$

As the branch shown in Figure 4, the vertices and edges of the parallel structure are depicted in green color. There are two simple paths between  $f_1$  and  $f_4$  whose transition probabilities are not equal to 1, but can add up to 1. Hence, vertices and edges in simple paths  $f_1e_1f_2e_3f_4$  and  $f_1e_2f_3e_4f_4$  form a branch structure. After completing  $f_1$ , the workflow continues with only one path in the branch, depending on the satisfied condition.

#### 3.2.3 Cycle

Considering all simple paths between vertices  $f_u \in V$  and  $f_v \in V$ , we define the subgraph  $G_c = (V_c, E_c)$  as a *cycle structure* between vertices  $f_u$  and  $f_v$ , where

$$V_c = \{f \in V : f \text{ is in s for some s} \in ASP(f_u, f_v)\}$$

 $E_{c} = \{e \in E : e \text{ is in s for some s} \in ASP(f_{u}, f_{v})\} \uplus \{(f_{v}, f_{u})\}$ such that

- $0 < P(f_v, f_u) < 1$ , invoking  $f_u$  again after completing  $f_v$  is a possible event;
- $-\sum_{s \in ASP(f_u, f_v)}^{N} TPP(s) = 1, \text{ transition probabilities of}$
- all simple paths between  $f_u$  and  $f_v$  sum up to 1;
- $SUB(f_u, f_v)$  is a DAG, the subgraph between  $f_u$  and  $f_v$  does not have any loops and cycles;
- $SPL(f_{str}, f_u) < SPL(f_{str}, f_v)$ , compared to  $f_v$ ,  $f_u$  is closer to the entry point;
- $-\sum_{\substack{(f_v, f_i) \in out(f_v) \\ \text{ties of all edges starting from } f_v \text{ add up to } 1.} P(f_v, f_i) = 1, \text{ the transition probabili-}$

As the cycle shown in Figure 4, vertices  $f_1$  and  $f_2$  and edges  $e_1$  and  $e_2$  form a cycle, depicted in orange color. After completing  $f_2$ , depending on the satisfied condition, the workflow will either invoke  $f_3$ , or enter the cycle by invoking  $f_1$ .

#### 3.2.4 Self-loop

A self-loop is a special case of cycle with only one vertex and one edge. Considering a function  $f_u$  connected by an edge  $(f_u, f_u)$  to itself, we define the subgraph  $G_l = (V_l, E_l) =$  $({f_u}, {(f_u, f_u)})$  as a *self-loop structure*, such that

- $0 < P(f_u, f_u) < 1$ , invoking  $f_u$  again after completing  $f_u$  is a possible event;
- $\sum_{(f_u,f_i)\in out(f_v)} P(f_u,f_i) = 1$ , the transition probabilities of all edges starting from  $f_u$  add up to 1.

As the self-loop depicted in red color shown in Figure 4, after accomplishing  $f_1$ , the workflow will either invoke  $f_2$ , or enter the self-loop by invoking  $f_1$  again.

#### 3.3 Performance Modeling

We propose a performance model to get the end-to-end response time of the serverless workflow. As M, NI, and C defined in  $G_s$  are relevant to cost instead of performance, we do not consider them in the performance model for brevity. Specifically, we only consider the following graph with part of elements in  $G_s$ , defined as

$$G_{perf} = (V, E, P, D, RT, RTTP)$$
<sup>(5)</sup>

With different methods for different structures, the performance model trims the graph of  $G_{perf}$  by removing, adding, and modifying vertices, edges and elements, and converts  $G_{perf}$  into a *probabilistic DAG*, denoted as  $G_{pr}$ . We define the probabilistic DAG as

$$G_{pr} = (V, E, P, D, RT, RTTP) \tag{6}$$

such that

- $G_{pr}$  is a DAG without any cycles and loops;  $\sum_{s \in ASP(f_{str}, f_{end})} TPP(s) = 1$ , the transition probabilities of all simple paths between the start node and

the end node in  $G_{pr}$  can sum up to 1.

The end-to-end response time of the serverless workflow  $G_{perf}$ , denoted as  $ERT(G_{perf})$ , is defined as Equation (7).

$$ERT\left(G_{perf}\right) = \sum_{s \in ASP(f_{str}, f_{end})} TPP\left(s\right) DLY\left(s\right) \quad (7)$$

where  $ASP(f_{str}, f_{end})$  is the set of all simple paths between the start node and end node in  $G_{pr}$ , which is the probabilistic DAG converted from  $G_{perf}$  by the proposed performance model.

To convert a serverless workflow into a probabilistic DAG, the model needs to remove cycles and self-loops from the workflow and trim parallel paths. In the following subsections, we describe how the performance model processes four types of structures in the serverless workflow and converts the workflow graph into a probabilistic DAG.

#### 3.3.1 Process branches

The workflow selects only one path in the branch depending on the satisfied condition. Each condition has a probability specified by the transition probability function. The main idea of processing the branch is to simplify the workflow by replacing branch paths with an interim B-node while retaining the information, including response time and the probability of each branch path.

Consider a branch  $G_b = (V_b, E_b)$  between vertices  $f_u$ and  $f_v$ , let SRT denote the response time of a structure, we can obtain the branch structure's expected value of the response time by Equation (8).

$$SRT(G_b) = \sum_{s \in ASP(f_u, f_v)} TPP(s) DLY(s)$$
(8)

After calculating the expected value of the delay, the performance model trims  $G_s$  by first removing all vertices in  $V_b$  except  $f_u$  and  $f_v$  from V, namely we get a smaller set of vertices, denoted as  $V^*$ , defined as

$$V^* = V \setminus (V_b \setminus \{f_u, f_v\})$$

Correspondingly, we remove all elements relevant to removed vertices by restricting functions as follows:

$$E^{*} = E \Downarrow V^{*}, P^{*} = P \Downarrow V^{*}, D^{*} = D \Downarrow V^{*}$$
$$RT^{*} = RT \Downarrow V^{*}, RTTP^{*} = RTTP \Downarrow V^{*}$$

Then, we add an interim vertex called "B-node", denoted as  $f_B$ , to V, and connect  $f_u$ ,  $f_B$ , and  $f_v$  in sequence by adding two edges  $(f_u, f_B)$  and  $(f_B, f_v)$  to E. We extend functions in the graph tuple as follows:

$$V' = V^* \uplus \{f_B\}, E' = E \ \uplus \{(f_u, f_B), (f_B, f_v)\}$$
$$P' = P^* [(f_u, f_B) \mapsto 1, (f_u, f_B) \mapsto 1]$$
$$D' = D^* [(f_u, f_B) \mapsto 0, (f_u, f_B) \mapsto 0]$$
$$RT' = RT^* [f_B \mapsto SRT (G_b) - RT (f_u) - RT (f_v)]$$

The above procedures simplify the workflow graph, as multiple vertices in the branch are replaced by an interim B-node, whose response time is the weighted average response time of branch paths. However, simply using the weighted average value would compromise the accuracy of the performance model. An example is when a branch is in parallel to other paths, as shown in Figure 5. Therefore, we retain the information, including response time and probability of each branch path using *RTTP* for later processing.

Specifically, we define RTTP as a function RTTP :  $V \rightarrow \wp([0,+\infty) \times [0,1])$ , which represents all possible values of the response time and corresponding probability of all original paths replaced by interim B-nodes. When processing branches and adding B-nodes, we have

$$RTTP' = RTTP^* [f_B \mapsto B]$$

where

$$B = \left\{ \left( {DLY^ - \left( s \right),TPP\left( s \right)} \right)|\forall s \in ASP\left( {{f_u},{f_v}} \right) \right\}$$

After processing branches, the workflow graph is updated as  $G_{perf} \leftarrow G' = (V', E', P', D', RT', RTTP').$ 

#### 3.3.2 Process parallels

For a given parallel structure  $G_p = (V_p, E_p)$  between vertices  $f_u$  and  $f_v$ , the workflow executes all parallel paths after completing  $f_u$  and invokes  $f_v$  only after finishing the executions of all paths. Hence, as shown in Equation (9), the response time of a parallel structure is the longest delay of parallel paths in it. Therefore, the main idea of processing



Fig. 5. Steps of the performance modeling algorithm solving the end-to-end response time of the serverless application shown in Figure 3. The interim B-node and P-node ( $B_1$ ,  $B_2$ ,  $P_1$ , and  $P_2$ ) are depicted in bold. The value of RTTP of the B-node retains the response time and probability of each path in the branch. The number on each edge represents the transition probability, and the transition delay is considered as zero for brevity.

the parallel is to retain the parallel path with the longest delay and prune other paths.

$$SRT(G_{p}) = \max \left\{ DLY(s) \mid \forall s \in ASP(f_{u}, f_{v}) \right\}$$
(9)

For a parallel structure without any interim B-nodes in any paths, the delay of each path is deterministic. We can directly use Equation (9) to get the delay of the parallel structure, which is also deterministic. However, if there are B-nodes in any paths, the delay of the parallel structure may have a probability distribution instead of being a fixed value. Since the response time of the B-node, recorded by *RTTP*, varies based on probabilities under different conditions, the delay of the path with B-nodes is subject to a probability distribution, making the delay of the parallel structure probabilistic. In this case, the performance model leverages Algorithm 1 to get a set of tuples, denoted as *RTTP\_List*, which has all possible values of response time and corresponding probabilities of the parallel structure.

After calculating the delay using Equation (9) or deriving  $RTTP\_List$ , similar to the trimming step in Section 3.3.1, the performance model removes all vertices in  $V_p$  except  $f_u$  and  $f_v$  from V, and then restricts functions. We have

$$V^* = V \setminus (V_p \setminus \{f_u, f_v\})$$
  

$$E^* = E \Downarrow V^*, P^* = P \Downarrow V^*, D^* = D \Downarrow V^*$$
  

$$RT^* = RT \Downarrow V^*, RTTP^* = RTTP \Downarrow V^*$$

Then, we add the interim vertex called "P-node" to V. If the parallel structure does not have any B-nodes, we only add one P-node, denoted as  $f_P$  and let

$$V' = V^* \uplus \{f_P\}, E' = E^* \uplus \{(f_u, f_P), (f_P, f_v)\}$$
  

$$P' = P^* [(f_u, f_P) \mapsto 1, (f_P, f_v) \mapsto 1]$$
  

$$D' = D^* [(f_u, f_P) \mapsto 0, (f_P, f_v) \mapsto 0]$$
  

$$RT' = RT^* [f_P \mapsto SRT (G_p) - RT (f_u) - RT (f_v)]$$

If  $V_p$  contains B-nodes, by using Algorithm 1, we have  $RTTP\_List = \{(rt_1, pr_1), (rt_2, pr_2), ..., (rt_M, pr_M)\}$ , which has M tuples of the response time and probability. Then, M P-nodes will be added as follows:

$$V' = V^* \uplus_{i=1}^{M} \{f_{P_i}\}, E' = E^* \uplus_{i=1}^{M} \{(f_u, f_{P_i}), (f_{P_i}, f_v)\}$$
  
for all  $1 \le i \le M$ :  
$$P' = P^* [(f_u, f_{p_i}) \mapsto pr_i, (f_{p_i}, f_v) \mapsto 1]$$
  
$$D' = D^* [(f_u, f_{p_i}) \mapsto 0, (f_{p_i}, f_v) \mapsto 0]$$
  
$$RT' = RT^* [f_{p_i} \mapsto tp_i]$$

After processing paralles, the workflow graph is updated as  $G_{perf} \leftarrow G' = (V', E', P', D', RT', RTTP')$ .

#### 3.3.3 Process cycles

For processing cycles, the main idea is to remove the cycle and add the delay incurred by cycle iterations to the last vertex's response time in the cycle. For a given cycle  $G_c = (V_c, E_c)$  between vertices  $f_u$  and  $f_v$ , the expected value of the number of cycle  $G_c$  iterations, denoted as  $EI(G_c)$ , namely the average number of times the workflow enters the cycle after completing  $f_v$ , can be expressed as Equation (10).

$$EI(G_c) = \sum_{n=1}^{\infty} [1 - P(f_v, f_u)] [P(f_v, f_u)]^{n-1} (n-1)$$
$$= \frac{P(f_v, f_u)}{1 - P(f_v, f_u)}$$
(10)

By multiplying the expected number of cycle iterations and the time required for each iteration, we can calculate the expected delay incurred by cycle iterations.

$$DI(G_c) = \left(\sum_{s \in ASP(f_u, f_v)} TPP(s) DLY(s) + D(f_v, f_u)\right) EI(G_c)$$

**Input:** a parallel  $G_p = (V_p, E_p)$  between  $f_u \in V_p$  and  $f_v \in V_p$  with n paths Output: a set of tuples *RTTP\_List* which has all possible values of response time and corresponding probability of  $G_P$ 1 for path  $s_i \in ASP(f_u, f_v)$  do  $RTTP\_List_i \leftarrow []; \triangleright \text{ results list}$ 2 if  $s_i$  has  $m \ge 1$  B-nodes  $\{f_{B_1}, f_{B_2}, ..., f_{B_m}\}$  then  $RT\_wo\_B \leftarrow DLY^-(s_i) - \sum_{k=1}^m RT(f_{B_k})$   $\triangleright$  the delay of the path without B-nodes 3 4  $cmb \leftarrow RTTP(f_{B_1}) \times ... \times RTTP(f_{B_m});$ 5  $\triangleright$  all combinations of the RT and prob. of all B-nodes by the Cartesian product for each combo  $C_j$  in cmb do 6  $RTC_j \leftarrow \sum_{(rt_k, tp_k) \in C_j} rt_k + RT\_wo\_B;$ 7  $\triangleright$  a possible response time of  $s_i$  $TP\dot{C}_{j} \leftarrow \prod_{(rt_{k}, tp_{k}) \in C_{j}}$  $tp_k$ ; 8  $\triangleright$  the corresponding probability append  $(RTC_j, TPC_j)$  to  $RTTP\_List_i$ ; 9 end 10 11 else ▷ the path that does not have any B-nodes  $RTC \leftarrow RT(s_i) - r_x - r_y; \triangleright \text{ RT is}$ 12 deterministic append (RTC, 1) to  $RTTP\_List_i$ ; > prob. is 1 13 end 14 15 end 16  $rttp\_comb \leftarrow RTTP\_List_1 \times ... \times RTTP\_List_n;$ 17  $RTTP\_List \leftarrow [];$ 18 for each combo  $C_j$  in  $rttp\_comb$  do  $RTC_j \leftarrow \max \{ rt_k | \forall (rt_k, tp_k) \in C_j \}; \triangleright \text{ a possible}$ 19 RT of  $G_p$  , use maximum value due to parallelism  $TPC_j \gets \prod_{(rt_k, tp_k) \in C_j} tp_k; \triangleright \text{ the corresponding prob.}$ 20 append  $(RTC_j, TPC_j)$  to  $RTTP\_List$ ; 21 22 end 23 return RTTP\_List

In terms of the response time of the cycle structure, the delay incurred by cycle iterations is equivalent to increasing the response time of  $f_v$  by the same amount of time. Therefore, the performance model first removes the edge  $(f_v, f_u)$  as

$$E' = E \setminus \{(f_v, f_u)\}$$

Then, the model modifies the transition probability, edge delay, and vertex response time as follows:

$$P^* = P\left[e \mapsto \frac{P(e)}{1 - P(f_v, f_u)}\right], \text{ for all } e \in out(f_v)$$
$$D' = D\left[(f_v, f_u) \mapsto 0\right], P' = P^*\left[(f_v, f_u) \mapsto 0\right]$$
$$RT' = RT\left[f_v \mapsto RT\left(f_v\right) + DI\left(G_c\right)\right]$$

After processing cycles, the workflow graph is updated as  $G_{perf} \leftarrow G' = (V, E', P', D', RT', RTTP).$ 

#### 3.3.4 Process self-loops

The procedure to process self-loops is similar to that used to process cycles. Given a self-loop  $G_l = (\{f_u\}, \{(f_u, f_u)\})$ , similarly using Equation (10), we can calculate the expected number of self-loop iterations as  $EI(G_l) = \frac{P(f_u, f_u)}{1 - P(f_u, f_u)}$ , and the delay incurred by self-loop iterations

as  $DI(G_l) = EI(G_l)(RT(f_u) + D(f_u, f_u))$ . Then, the performance model updates the graph as  $G_{perf} \leftarrow G' = (V, E', P', D', RT', RTTP)$ , where

$$P^{*} = P\left[e \mapsto \frac{P(e)}{1 - P(f_{u}, f_{u})}\right], \text{ for all } e \in out(f_{u})$$
$$D' = D\left[\left(f_{u}, f_{u}\right) \mapsto 0\right], P' = P^{*}\left[\left(f_{u}, f_{u}\right) \mapsto 0\right]$$
$$E' = E \setminus \left\{\left(f_{u}, f_{u}\right)\right\}$$
$$RT' = RT\left[f_{u} \mapsto RT\left(f_{u}\right) + DI\left(G_{l}\right)\right]$$
(11)

#### 3.4 Cost Modeling

In this section, we introduce a cost model to get the average cost of the serverless workflow. Since FaaS platforms leverage a GB-second billing model depending on the allocated memory size, rounded-up function duration, and the number of invocations, we consider the following graph with part of elements in  $G_s$ , defined as

$$G_{\cos t} = (V, E, P, RT, M, NI, C)$$
(12)

Algorithm 2: Performance modeling algorithm **Input:** a serverless workflow  $G_s = (V_s, E_s)$ Output: the average end-to-end response time of the serverless application 1  $G' \leftarrow G_s;$ **2** while G' is not a probabilistic DAG (using eq. (6)) do loop\_list  $\leftarrow$  find\_self\_loops(G');  $\triangleright$  section 3.2.4 3 **for** each self-loop  $G_i$  in loop\_list **do** 4 5 Process self-loop  $G_i$ ; > Section 3.3.4 end 6 7  $cycle_list \leftarrow find_cycles(G'); \triangleright section 3.2.3$ **for** each cycle G<sub>i</sub> in self\_loop\_list **do** 8 Process cycle  $G_i$ ; > Section 3.3.3 9 10 end 11  $parallel\_list \leftarrow find\_parallels(G'); \triangleright section 3.2.1$ **for** each parallel  $G_i$  in parallel\_list **do** 12 Process parallel G<sub>i</sub>; ▷ Section 3.3.2 13 14 end branch\_list  $\leftarrow$  find\_branches(G');  $\triangleright$  section 3.2.2 15 for each branch  $G_i = (V_i, E_i)$  in branch\_list do 16 Process branch G<sub>i</sub>; ▷ Section 3.3.1 17 18 end 19 end  $\sum_{s \in ASP_{G'}(f_{str}, f_{end})} TPP(s) \cdot DLY(s); \triangleright \text{ eq. (7)}$ 20  $ERT \leftarrow$ 21 return ERT

All vertices representing FaaS functions have an amount of allocated memory, identified by M. The allocated memory of 0 represents such vertex might be a structural node without any cost, like start and end nodes, or other cloud services to which the GB-second billing model is not applicable. The rounded-up function duration can be directly calculated using the response time of each function defined by RT. For a FaaS function  $f_u \in V$ , its average cost, per application execution, can be calculated as Equation (13), where PGS is the price per GB-second and PPI is the price per invocation (the cost of handling the invocation request). For vertices representing cloud services with other pricing models, the model obtains their cost from users' input.

$$C(f_u) = NI(f_u) \left( \left\lceil \frac{RT(f_u)}{100} \right\rceil \cdot M(f_u) \cdot PGS + PPI \right)$$
(13)

Each vertex  $f_u \in V$  has an average number of invocations, denoted as  $NI(f_u)$ , which depends on the structure of the serverless workflow. Branches can reduce the number of invocations of vertices in them, since the transition probability of paths in branches is less than 1. Conversely, cycles and self-loops can lead to more than once invocation of functions in them, and the number of invocations depends on the expected value of the number of cycle/self-loop iterations, calculated as Equation (10). Hence, for a given cycle  $G_c = (V_c, E_c)$  between vertices  $f_u$  and  $f_v$ , we have the expected value of the number of invocations of each vertex  $f_i \in V_c$  as

$$NI(f_i) = 1 + EI(G_c) = \frac{1}{1 - P(f_v, f_u)}, \forall f_i \in V_c \quad (14)$$

Similarly, for a self-loop  $G_l = (\{f_u\}, \{(f_u, f_u)\})$ , we have

$$NI(f_u) = 1 + EI(G_l) = \frac{1}{1 - P(f_u, f_u)}$$
(15)

The cost model first leverages Equation (14) and Equation (15) to calculate the average number of invocations of vertices in cycles and self-loops. Then, similar to procedures of processing cycles and self-loops in the performance model, the cost model updates the edge and transition probability to remove cycles and self-loops, considering the impact of parallels and branches, the cost model updates NI of each vertex based on the sum of transition probabilities of all simple paths from the start node to it. By following these steps, we convert  $G_{cost}$  into a de-looped graph used for cost modeling, denoted as  $G_{dl}$ . The average cost of the serverless workflow can be calculated by  $\sum_{f \in V} C(f)$ . Algorithm 3 gives the pseudo-code of the cost model.

#### 3.5 Summary, Example, and Analysis

The implementation of the performance model is presented in Algorithm 2. Based on definitions of structures in the serverless workflow, as mentioned in Section 3.1, the algorithm identifies structures in the workflow and leverages different procedures to process structures, defined in Section 3.3, to trim the workflow graph to a probabilistic DAG and obtain the end-to-end response time of the application. Figure 5 illustrates the step-by-step changes of the workflow graph when the performance model works on the serverless workflow shown in Figure 3. The average end-to-end response time of the application is 2111.11ms.

Algorithm 3 describes the implementation of the cost model. Taking the serverless workflow showing in Figure 3 as an example, after completing the first while loop, the algorithm trims the workflow to a de-looped graph shown in Figure 6. Then, in the for loop, the algorithm updates the average number of invocations for each function again and calculates the cost of the applications. The average cost of the application is \$41.82 per 1 million executions.

Let us consider the worst case scenario and analyze the time complexities of the performance and cost models. Under the definition of the serverless workflow mentioned in 3.1, the most complex workflow is composed of as many cycles and self-loops as possible, since the cycle and self-loop structures require the least number of vertices,



Fig. 6. The de-looped workflow of the serverless application shown in Figure 3. The three numbers on each function represent the response time, allocated memory and average number of invocations, respectively. The number on each edge represents the transition probability.

Algorithm 3: Cost modeling algorithm				
<b>Input:</b> a workflow graph $G_{cost}$				
Output: the average cost for each execution of the				
serverless application				
1 $G' \leftarrow G_{cost};$				
2 for all $f \in V$ , let $NI(f) \leftarrow 1$ ; $\triangleright$ initialization				
3 while G' is not a DAG do				
4   loop_list $\leftarrow$ find_self_loops(G'); $\triangleright$ section 3.2.4				
5 <b>for</b> self-loop $G_l = (f_u, (f_u, f_u))$ in loop_list <b>do</b>				
6 $NI(f_u) \leftarrow \frac{1}{1 - P(f_u, f_u)}; \triangleright \text{ eq. (15)}$				
7 $E \leftarrow E \setminus \{(f_u, f_u)\}; \triangleright$ remove the loop edge				
s for each edge $e$ in $out(f_u)$ do				
9 $P \leftarrow P \left[ e \mapsto \frac{P(e)}{1 - P(f_w, f_w)} \right]; \triangleright \text{ updat prob.}$				
10 end				
11 end				
12 cycle_list $\leftarrow$ find_cycles(G');				
13 <b>for</b> each cycle $G_i = (V_i, E_i)$ in cycle_list <b>do</b>				
14 For each $f \in V_i$ update $NI(f)$ using eq. (14);				
15 Remove the cycle edge;				
16 Update transition probabilities of outgoing				
edges;⊳ similar to steps for self-loops				
17 end				
18 end				
19 for each vertex $f \in V$ do				
20 $tp\_sum \leftarrow \sum_{(A,B,D) = (f, f, f)} TPP(s);$				
if the sum < 1 then				
$\begin{array}{c c} 1 & i \ i \ i \ j \ j \ sum \\ \hline \end{array} \\ \hline \begin{array}{c} 1 & i \ i \ l \ j \ sum \\ \hline \end{array} \\ \hline \end{array} \\ \hline \begin{array}{c} 1 & i \ l \ l \ sum \\ \hline \end{array} \\ \hline \end{array} \\ \hline \begin{array}{c} 1 & i \ l \ l \ sum \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \begin{array}{c} 22 & i \ l \ sum \\ \hline \end{array} \\ \hline \end{array} \\ \hline \begin{array}{c} 1 & i \ l \ sum \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \begin{array}{c} 22 & i \ sum \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \begin{array}{c} 22 & i \ sum \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \begin{array}{c} 1 & i \ sum \\ \hline \end{array} \\ \\ \hline \end{array} \\ \\ \hline \end{array} \\ \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \\ \\ \hline \end{array} \\ \\ \hline \end{array} \\ \\ \\ \hline \end{array} \\ \\ \\ \hline \end{array} $ \\ \hline \\ \\ \end{array} \\ \\ \hline \end{array} \\ \\ \\ \\ \end{array} \\ \\ \end{array} \\ \\ \hline \end{array} \\ \\ \\ \\				
$23 \mid \text{end}$				
24 $cost sum \leftarrow cost sum + C(f); \triangleright eq. (13)$				
25 end				
26 return cost sum				

compared to the parallel and branch structures. Figure 7 illustrates the workflow under the worst case scenario, where the workflow is composed of n functions, (n + 2)vertices,  $\frac{n(n+3)+2}{2}$  edges,  $\frac{n(n-1)}{2}$  cycles, and *n* self-loops. The time complexities for detecting self-loops and cycles are O(|E|) and O(C(|V| + |E|)), respectively, where C is the number of cycles. The performance model and cost model can process cycles and self-loops in  $O(n^2)$  and O(n) time, respectively. Hence, the time complexities for the performance and cost modeling under the worst case scenario are  $O(n^6)$  and  $O(n^5)$ , respectively, where n is the number of functions in the workflow. We empirically analyze the AWS and Azure official repositories [30], [31]. The average number of functions in serverless applications in this repository, orchestrated by Amazon Step Functions or Microsoft Azure Functions, is less than 5. We do not find



Fig. 7. The workflow of the worst case, which contains n functions, (n + 2) vertices,  $\frac{n(n+3)+2}{2}$  edges,  $\frac{n(n-1)}{2}$  cycles, and n self-loops.

any serverless application in the repositories resembling the worst case topology. The most common typologies appear to be sequential, paralleled, and branched. Our proposed models can calculate the performance and cost of a worst-case topology application with 27 functions and 406 edges in less than a second on a laptop with a 2.70GHz Intel Core i7-3740QM processor and 16 GB of memory. This shows the applicability of the models for now and a foreseeable future.

#### 4 PERFORMANCE AND COST OPTIMIZATION

As mentioned in Section 2, the response time of the function varies with the allocated memory, and so does the cost. Therefore, developers can tune the performance and cost of the serverless application by changing the allocated memory size of functions in the application. More specifically, as described by RQ2, very practical problems in serverless computing are to get the best performance under a limited budget or satisfy the performance constraint by the minimum cost. RQ2 leads to two performance and cost optimization problems. To answer them, we introduce the performance profile, define the optimization problem and propose an optimization algorithm in this section.

#### 4.1 Performance Profile of Serverless Functions

On FaaS platforms, increasing the memory of a function can improve the CPU and IO performance, but it does not necessarily reduce the response time of the function significantly, especially when the performance becomes insensitive to the memory when the amount is large enough. As shown in Figure 2, when the allocated memory is greater than 1792MB, the response time remains almost the same, and at this time, the continued increase in memory size incurs additional cost due to the rounding and granularity of billed duration. Similarly, albeit larger allocated memory size leads to a higher price per second of billed duration, the cost may decrease with larger memory, especially before the performance becomes insensitive. For the performance-memory curve of functions, as the allocated memory size increases, response time decreases first and then levels out, since the performance becomes insensitive. However, because of the rounding and billing granularity, there are large fluctuations in the cost-memory curve of functions.

Therefore, as mentioned in the best practices for working with AWS Lambda Functions, to find an optimal allocated memory size satisfying both the trade-off between performance and price and the required memory size for the function execution, a performance profiling phase is highlyrecommended to test the performance of the FaaS functions [32]. In the performance profiling phase, the function is invoked using the payload with the average input size multiple times under different allocated memory size, and the average duration of invocations is logged. By doing so, we can acquire a set of viable memory size and a series of function response time under different memory sizes. Figure 2 demonstrates the performance-memory curve of a function obtained in the performance profiling phase. Explicitly, we let *MOpt* denote a memory option function mapping the function to its viable memory options, defined as Equation (16).

$$MOpt: V \to \wp(\mathbb{N})$$
 (16)

The performance profile of a function  $f_u$ , which describes the response time of the function under different allocated memory sizes, is defined as Equation (17).  $PF(f_u, mem_v)$  is the response time of  $f_u$  with the allocated memory size of  $mem_v$ , where  $f_u \in V$  and  $mem_v \in MOpt(f_u)$ .

$$PF: \underset{f \in V}{\textcircled{\ }} \{\{f\} \times MOpt(f)\} \to [0, +\infty)$$
(17)

Considering the performance profile of functions, in this section, we extend the definition of serverless workflow as

$$G_s = (V, E, P, D, RT, RTTP, M, NI, C, MOpt, PF)$$

where *MOpt* and *PF* are defined as Equation (16) and Equation (17), respectively. Let  $MOpt(f) \triangleq \emptyset$  for all *f* is not a FaaS function.

#### 4.2 Problem Statement

Considering a serverless workflow  $G_s$  with n functions, where  $V = \{f_1, f_2, ..., f_{n-1}, f_n\}$ , we define  $\pi$  as a memory configuration of the workflow, such that

$$\pi \in MOpt(f_1) \times MOpt(f_2) \times ... \times MOpt(f_n)$$

 $\pi(f)$  denotes the size of the allocated memory of the function f in this configuration. Let  $ERT^{\pi}$  denote the endto-end response time of  $G_s$  obtained by the performance model and  $C^{\pi}(f_u)$  denote the cost of the function  $f_u$  obtained by the cost model, under the memory configuration  $\pi$ , such that (i)  $M(f_i) = \pi(f_i)$ , for all  $1 \leq i \leq n$ , (ii)  $RT(f_i) = PF(f_i, \pi(i))$ , for all  $1 \leq i \leq n$ . For a given budget limit BC, and a performance constraint PC, we define the following two optimization problems.

## 4.2.1 Best Performance under Budget Constraint (BPBC)

Find a memory configuration  $\pi$  that achieves the minimum average end-to-end response time of the application with the average cost less than or equal to the budget *BC*.

SU

$$\underset{\pi}{\operatorname{arg\,min}} \quad ERT^{\pi}\left(G_{s}\right)$$

$$bject \ to \quad \sum_{i=1}^{n} C^{\pi}(f_{i}) \leq BC$$
(18)

#### 4.2.2 Best Cost under Performance Constraint (BCPC)

Find a memory configuration  $\pi$  that achieves the minimum average cost of the application with the average end-toend response time less than or equal to the performance constraint *PC*.

$$\underset{\pi}{\operatorname{arg\,min}} \quad \sum_{i=1}^{n} C^{\pi}(f_i)$$
subject to  $ERT^{\pi}(G_s) \leq PC$ 
(19)

#### 4.3 Problem Complexity Analysis

We prove that BPBC and BCPC problems in the serverless computing paradigm are fundamentally more complex variants of the multiple-choice knapsack problem (MCKP). MCKP is formulated as follows. Given n sets  $\mathbb{N}_1, \mathbb{N}_2, ..., \mathbb{N}_n$ of items, where each item in each set has a profit and a weight, by selecting exactly one item from each set, the optimization problem is to find a selection combination  $\varsigma \in \mathbb{N}_1 \times \mathbb{N}_2 \times ... \times \mathbb{N}_n$  such that  $\varsigma$  maximizes the total profit while the total weight within the capacity. MCKP has been applied to many optimization problems, including resource allocation and workflow optimization in the parallel computing and microservice-based applications [33], [34].

In BPBC and BCPC problems, the n functions, viable allocated memory sizes of each function *MOpt*, and the memory configuration  $\pi$  are equivalent to *n* sets, a number of items in each set, and selection combination  $\varsigma$  in MCKP, respectively. For the BPBC problem, BC corresponds to the knapsack capacity constraint,  $-PF(f, M_k)$  can be viewed as the profit of the function  $f \in V$  with the allocated memory size of  $M_k \in MOpt(f)$ , and corresponding cost C(f) is equivalent to the weight. Instead of simply accumulating values, the total profit in the BPBC problem, represents the end-to-end response time of the application, should be derived by the performance modeling algorithm defined in Algorithm 2. Similarly, for the BCPC problem, PC corresponds to the knapsack capacity constraint, the cost C(f)of the function f under the memory  $M_k \in MOpt(f)$  can be viewed as the profit of the function, the response time  $PF(f, M_k)$  can be deemed as the weight.

Compared to MCKP, the higher complexity of BPBC and BCPC problems lies in calculating the total profit and total weight, which leverages the polynomial-time performance and cost models defined in Section 3. Besides, for a given memory configuration and corresponding response time, we can check whether the average end-to-end response time and total cost under such a configuration satisfy the constraints in polynomial time. Hence, BPBC and BCPC problems in the serverless computing paradigm are fundamentally more complex variants of MCKP.

As MCKP has proven to be a NP-complete problem without any solutions in polynomial time, unless P = NP [35], we have to resort to a heuristic algorithm to solve BPBC and BCPC problems.

#### 4.4 Probability Refined Critical Path Algorithm (PRCP)

In this section, we propose a heuristic algorithm based on the critical path method to solve BPBC and BCPC problems.

### 4.4.1 Critical Path Method

Critical path method (CPM) is a heuristic approach for scheduling problems, which optimizes the scheduling scheme by identifying and rescheduling the path with the longest execution time [36]. CPM has proven to be an effective solution to scheduling problems in many areas including the scientific workflow system [33], distributed computing framework [37], IaaS paradigm [38], and CaaS paradigm [34]. However, previous studies have largely applied CPM to DAG workflows. As mentioned in Section 2, there can be cycles and loops in the serverless workflow, to which the traditional CPM is not applicable.

#### 4.4.2 Algorithm Design

We propose a Probability Refined Critical Path Algorithm (PRCP) to solve BPBC and BCPC optimization problems for non-DAG serverless workflows. To work with non-DAG workflow topology, PRCP refines the transition probability of edges and simple paths as well as the weight of simple paths based on the transition probability, and leverages a weight-based definition of the critical path. PRCP recursively optimizes the memory of functions on the critical path using a greedy manner and obtains the best memory configurations satisfying the constraint.

Based on the definition of the serverless workflow, due to transition probabilities and structures in the workflow, the path with the longest delay may not be the critical path in terms of the response time and cost. Therefore, we need to re-define the critical path to take the transition probability of the path and iterations incurred by cycles and loops into account.

For a simple path  $s_k = f_1 e_1 f_2 e_2 \dots e_{n-1} f_n$ , we define the weight of  $s_k$  as Equation (20).

$$W(s_k) = \sum_{i=1}^{n} RT(f_i) NI(f_i) TPP(s_k)$$
(20)

Given a set of M simple paths, we define the path with  $i^{th}$  greatest weight as the  $i^{th}$  critical path, such that  $1 \le i \le M$ . We denote FindCriticalPath(G, i) as a procedure which returns the  $i^{th}$  critical path in G.

Given a function  $f_u$  and a new memory size  $mem_v \in MOpt(f_u)$ , by assigning the new allocated memory size  $mem_v$  to  $f_u$ , we define the change of end-to-end response time and the change of cost, as  $\Delta ERT(f_u, mem_v)$  and  $\Delta C(f_u, mem_v)$ , respectively, where

$$\Delta ERT (f_u, mem_v) = ERT^{\gamma} (G_s) - ERT_{curr}$$
$$\Delta C (f_u, mem_v) = \sum_{i=1}^n C^{\gamma} (f_i) - C_{curr}$$

such that (i)  $ERT_{curr}$  and  $C_{curr}$  are the end-to-end response time and cost under the previous configuration  $\pi$ ; (ii)  $\gamma(f_u) = mem_v$ ; (iii)  $\gamma(f_i) = \pi(f_i)$  for all  $1 \le i \le n$  and  $i \ne u$ .

Algorithm 4 demonstrates the pseudocode of the PRCP algorithm solving the BPBC problem. The input are the budget constraint BC and a serverless workflow  $G_s$  with n functions, where  $V = \{f_1, f_2, ..., f_{n-1}, f_n\}$ . PRCP first initializes the workflow by employing the minimum memory configuration  $\pi_{min}$ , such that  $\pi_{min}(f_i) = \min(MOpt(f_i))$ 

for all  $1 \leq i \leq n$ . The workflow has the largest end-toend response time under the minimum memory configuration. PRCP recursively finds the critical path and calculates  $\Delta ERT$  and  $\Delta C$  under all possible allocated memory size of all functions in the critical path. If there are functions and memory size options that can reduce the cost without increasing the end-to-end response time of the workflow, namely  $\Delta C < 0$  and  $\Delta ERT \leq 0$ , PRCP selects the function and memory size resulting in the largest cost decrease. If not, PRCP chooses the function and memory size achieving the largest end-to-end response time decrease within the budget constraint. If there is no feasible memory size option within the  $t^{th}$  critical path, where t is initialized as 1, PRCP will find the  $(t+1)^{th}$  critical path in the next iteration, and so on. The iteration ends when there is no feasible memory size option in the least critical path with the current surplus.

Algorithm 4: PRCP-BPBC

Input: Budget constraint BC, serverless workflow  $G_s = (V, E, P, D, RT, RTTP, M, NI, C, MOpt, PF)$ **Output:** memory configuration  $\pi$  satisfying eq. (18) 1  $M \leftarrow M \left[ f \mapsto \min \left( MOpt \left( f \right) \right) \right], \forall f \in V; \triangleright$  use the minimal memory configuration  $\pi_{min}$  2  $G_{dl} \leftarrow (V, E', P', RT, M, NI, C, MOpt, PF); \triangleright$  Get the de-looped graph using steps in Section 3.4 3  $NSP \leftarrow |ASP_{G_{dl}}(f_{str}, f_{end})|; \triangleright$  number of simple paths in  $G_{dl}$ 4  $\pi_{curr} \leftarrow \pi_{min}; \triangleright$  current memory configuration 5  $C_{curr} \leftarrow \sum_{i=1}^{n} C^{\pi_{min}}(f_i); \triangleright$  current cost 6  $ERT_{curr} \leftarrow ERT^{\pi_{min}}(G_s); \triangleright$  current end-to-end RT 7  $t \leftarrow 1$ ; s while  $BC - C_{curr} > 0$  and  $t \le NSP$  do  $s_{cp} \leftarrow FindCriticalPath(G_{dl}, t); \triangleright \text{ find } t^{th}$ 9 critical path in  $G_{dl}$ for all functions  $f_i$  in  $s_{cp}$  do 10 for all selectable memory  $mem_i \in MOpt(f_i)$  do 11 Calculate  $\Delta ERT(f_i, mem_j)$  and 12  $\Delta C(f_i, mem_i);$ 13 end end 14 if  $\exists mem_v \in MOpt(f_u): \Delta ERT(f_u, mem_v) \leq 0$  and 15  $\Delta C(f_u, mem_v) < 0$  then  $f_{tmp}, mem_{tmp} \leftarrow \arg\min\Delta C\left(f_u, mem_v\right);$ 16  $f_u, mem_v$ else 17  $f_{tmp}, mem_{tmp} \leftarrow \arg\min\Delta ERT\left(f_u, mem_v\right)$ 18  $f_u, mem_v$ s.t.  $\Delta C(f_u, mem_v) \leq BC - C_{curr}$  and  $\Delta ERT(f_u, mem_v) < 0$ . If there are multiple functions and memory values that achieve the same maximum  $\Delta ERT$ , select  $f_u$  and  $mem_v$ that leads to the smallest  $\Delta C$ ; end 19 20 if  $f_{tmp}$  and  $mem_{tmp}$  exist then  $M \leftarrow M [f_{tmp} \mapsto mem_{tmp}];$ 21  $RT \leftarrow RT [f_{tmp} \mapsto PF (f_{tmp}, mem_{tmp})];$ 22  $\pi_{curr} \leftarrow \pi_{curr} \left( f_{tmp} \right) \triangleq mem_{tmp};$ 23  $C_{curr} \leftarrow C_{curr} + \Delta C \left( f_{tmp}, mem_{tmp} \right);$ 24 25  $ERT_{curr} \leftarrow ERT_{curr} + \Delta ERT (f_{tmp}, mem_{tmp});$ 26 else 27  $t \leftarrow t + 1;$ end 28 29 end 30 return  $\pi_{curr}$ 

Algorithm 5 provides the pseudocode of the PRCP algorithm solving the BCPC problem. For the the BCPC problem, PRCP algorithm first initializes the workflow by employing the maximum memory configuration  $\pi_{max}$ , such that  $\pi_{\max}(f_i) = \max(MOpt(f_i))$  for all  $1 \le i \le n$ . The workflow has the smallest end-to-end response time under the maximum memory configuration. PRCP recursively finds the critical path, but starts with the path with the smallest weight, then calculates  $\Delta ERT$  and  $\Delta C$  under all possible allocated memory size of all functions in that path. If there are functions and memory size options that can reduce the end-to-end response time of the workflow without incurring additional cost, namely  $\Delta ERT < 0$  and  $\Delta C \leq 0$ , PRCP selects the function and memory size leading to the largest end-to-end response time decrease. If not, PRCP chooses the function and memory size resulting in the largest cost decrease within the performance constraint. If there is no feasible memory size option within the  $t^{th}$  critical path, where t starts with the number of simple paths in  $G_{dl}$ , PRCP will find the  $(t-1)^{th}$  critical path in the next iteration, and so on. The iteration ends when there is no feasible memory size option even in the most critical path with the current surplus in terms of the performance.

#### 4.4.3 Benefit/Cost Ratio (BCR) Greedy Strategies

PRCP algorithm is essentially a greedy heuristics for BPBC and BCPC problems. The steps with a box in Algorithm 4 and Algorithm 5 are greedy strategies. For instance, in the BPBC problem, the greedy strategy is to find the  $f_u$  and  $mem_v \in MOpt(f_u)$  in each critical path iteration, which can lead to the greatest end-to-end response time reduction. However, the local optimization achieved by such a strategy might compromise the global optimization. As mentioned in Section 4.1 and shown in Figure 2, after the performance becomes insensitive to the memory, the performance gain of the function brought by the increase in memory is insignificant, and due to rounding and billing granularity, the cost may increase significantly.

To avoid bad optimization solutions, we introduce the benefit/cost ratio (BCR) into greedy strategies. Instead of arbitrarily maximizing the end-to-end response time reduction, the strategy is to find the configuration achieving the optimal BCR. In other words, the idea is to find the configuration leading to the optimal benefit for its cost. We propose three BCR greedy strategies for each optimization problem and integrate them into the PRCP algorithm. For the BPBC problem, strategies are MAX, ERT/C, and RT/M. For the BCPC problem, strategies are MAX, C/ERT, and M/RT.

In the MAX strategy for the BPBC problem, the reduction on end-to-end response time is the benefit, and the cost is the increased cost of the workflow incurred by the configuration. Namely, for the function  $f_u$  and a selectable memory size  $mem_v \in MOpt(f_u)$ , BCR is defined as

$$BCR(f_u, mem_v) = \left| \frac{\Delta ERT(f_u, mem_v)}{\Delta C(f_u, mem_v)} \right|$$
(21)

The *MAX* strategy finds the  $f_u$  and  $mem_v \in MOpt(f_u)$  in each critical path iteration leading to the maximum BCR, which is defined as Equation (21).

The ERT/C strategy has the same definitions of the benefit and cost as the MAX strategy. A BCR threshold,

and Algorithm 5 are greedy strate BPBC problem, the greedy strate BPBC problem, the greedy strate  $mem_v \in MOpt(f_u)$  in each critican lead to the greatest end-to-end However, the local optimization ac might compromise the global optiin Section 4.1 and shown in Figure becomes insensitive to the memory the function brought by the increaicant, and due to rounding and bimay increase significantly.  $(f_u, mem_v) \leq 0$  and  $(f_u, mem_v);$   $(f_u, mem_v);$ 

#### Algorithm 5: PRCP-BCPC

	<b>Input:</b> Performance constraint <i>PC</i> , serverless					
	workflow					
	$G_s = (V, E, P, D, RT, RTTP, M, NI, C, MOpt, PF)$					
	<b>Output:</b> memory configuration $\pi$ satisfying eq. (18)					
1	$M \leftarrow M\left[f \mapsto \max\left(MOpt\left(f\right)\right)\right], \forall f \in V; \triangleright \text{ use the }$					
2	minimal memory configuration $\pi_{max}$ $G_{dl} \leftarrow (V, E', P', RT, M, NI, C, MOpt, PF); \triangleright$ Get the deployed graph using steps in Section 3.4					
3	$NSP \leftarrow  ASP_{G_{dl}}(f_{str}, f_{end}) ; \triangleright$ number of simple					
4	paths in $G_{dl}$ , $\pi_{curr} \leftarrow \pi_{max};  ightarrow$ current memory configuration					
5	$C_{curr} \leftarrow \sum_{i=1}^{n} C^{\pi_{max}}(f_i); \triangleright$ current cost					
6	$ERT_{curr} \leftarrow ERT^{\pi_{max}}(G_s); \triangleright \text{ current end-to-end RT}$					
7	$t \leftarrow 105r;$ while $PC = EPT = > 0$ and $t > 1$ do					
8	while $F C = E R I_{curr} > 0$ und $t \ge 1$ do					
,	$S_{cp}$ $(1)$ $($					
10	for all functions $f_i$ in $s_{cn}$ do					
11	<b>for</b> all selectable memory $mem_i \in MOpt(f_i)$ <b>do</b>					
12	Calculate $\Delta ERT(f_i, mem_i)$ and					
	$\Delta C(f_i, mem_i);$					
13	end					
14	end					
15	<b>if</b> $\exists mem_v \in MOpt(f_u): \Delta C(f_u, mem_v) \le 0$ and $\Delta EBT(f_u, mem_v) \le 0$ <b>then</b>					
16	$\begin{cases} f_{tmp}, mem_{tmp} \leftarrow \arg\min \Delta ERT(f_u, mem_v); \\ f_{tmp}, mem_{tmp} \leftarrow \arg\min \Delta ERT(f_u, mem_v); \end{cases}$					
17	else					
18	$f_{tmp}, mem_{tmp} \leftarrow \arg\min_{f_{tmp}} \Delta C\left(f_{u}, mem_{v}\right)$					
	$\int \int \int \int DT (f_{u}, mem_{v}) \leq DC = EDT$ and					
	S.L. $\Delta ERI(J_u, mem_v) \leq PC - ERI_{curr}$ and $\Delta C(f_mom_v) < 0$ If there are multiple					
	$\Delta C(J_u, mem_v) \leq 0$ . If there are intuitiple functions and momory values that achieve the					
	same minimum $\Delta C$ select f and mem that					
	leads to the smallest $\Delta ERT$ .					
19	end					
20	<b>if</b> $f_{tmp}$ and $mem_{tmp}$ exist <b>then</b>					
21	$M \leftarrow M [f_{tmp} \mapsto mem_{tmp}];$					
22	$RT \leftarrow RT [f_{tmp} \mapsto PF (f_{tmp}, mem_{tmp})];$					
23	$\pi_{curr} \leftarrow \pi_{curr} (f_{tmp}) \triangleq mem_{tmp};$					
24	$C_{curr} \leftarrow C_{curr} + \Delta C (f_{tmp}, mem_{tmp});$					
25	$  ERT_{curr} \leftarrow ERT_{curr} + \Delta ERT (f_{tmp}, mem_{tmp});$					
26	else					
27	$  t \leftarrow t - 1;$					
28	end					
29	end					
30	return $\pi_{curr}$					

denoted as TH, is leveraged. The ERT/C strategy keeps a record of the BCR of the configuration in the previous critical path iteration, denoted as  $BCR_{pre}$ . Instead of simply maximizing BCR, the ERT/C strategy finds  $f_u$  and  $mem_v \in MOpt(f_u)$  that results in the maximum BCR such that  $BCR \geq BCP_{pre} \cdot TH$ .

In the RT/M strategy, we introduce a BCR threshold TH and consider the two-point slope of the performancememory curve as the BCR, namely

$$BCR\left(f_{u}, mem_{v}\right) = \frac{PF\left(f_{u}, mem_{v+1}\right) - PF\left(f_{u}, mem_{v}\right)}{mem_{v+1} - mem_{v}}$$
(22)

where  $mem_{v+1} \in MOpt(f_u)$  is the adjacent selectable memory size such that  $mem_{v+1} > mem_v$ . For each function

TABLE 2 Summary of BCR Greedy Strategies. It contains BCR, optimization goal in each iteration, and the conditions to which the optimization is subject.

Strategy	BCR Def.	Maximize	Subject To
		BPBC Proble	т
W/O BCR MAX ERT/C RT/M	N/A eq. (21) eq. (21) eq. (22)	ERT Red. BCR BCR ERT Red.	None None $BCR \ge BCR_{pre} \cdot TH$ $BCR(f_i, mem_j) \ge \beta(f_i) \cdot TH$
		BCPC Proble	m
W/O BCR MAX C/ERT M/RT	N/A eq. (21) <sup>-1</sup> eq. (21) <sup>-1</sup> eq. (22) <sup>-1</sup>	Cost Red. BCR BCR Cost Red.	None None $BCR \ge BCR_{pre} \cdot TH$ $BCR(f_i, mem_j) \ge \beta(f_i) \cdot TH$

 $f_i \in V$ , the RT/M strategy algorithm first calculates the slope of the performance-memory curve by the least squares regression, denoted as  $\beta(f_i)$ . Then, the algorithm removes all memory options from the viable memory options whose BCR is smaller than  $\beta(f_i) \cdot TH$ . After this step, the memory option function satisfies  $\beta(f_i) \cdot TH$  for all  $1 \leq i \leq n$  and all  $mem_i \in MOpt(f_i)$ . In each critical path iteration, the algorithm finds the  $f_u$  and  $mem_v \in MOpt(f_u)$  resulting in the greatest end-to-end response time reduction.

Correspondingly, MAX, C/ERT and M/RT are three BCR greedy strategies for the BCPC problem, where the BCR is defined as the multiplicative inverse of the BCR defined for the BPBC problem. In the M/RT strategy, the algorithm calculates the slope of the memory-performance curve. Table 2 gives the summary of the original PRPC algorithm and BCR greedy strategies. Besides the s.t. conditions mentioned in Table 2, as specified in the pseudocode of the PRPC algorithm, all strategies should also satisfy  $\Delta C(f_u, mem_v) \leq BC - C_{curr}$  and  $\Delta ERT(f_u, mem_v) < 0$ for the BPBC problem, and  $\Delta ERT(f_u, mem_v) \leq PC ERT_{curr}$  and  $\Delta C(f_u, mem_v) < 0$  for the BCPC problem.

#### 4.4.4 Time Horizon of Modeling and Optimization

The proposed models and optimization algorithms can be updated by new monitoring data depending on the degree of uncertainty in the underlying FaaS infrastructure and the serverless application itself. However, if the initial performance profiling phase has been done properly, the performance and cost models and optimal configurations should remain valid for a long time. Other reasons for updating the model will be changing the function configurations, the application architecture, function source code, or optimization constraints. From a practical point of view, these parameters are not expected to change frequently. Suppose any of the parameters mentioned above, except function source code, changes. In that case, users only need to rerun performance and cost models and optimization algorithms, which can be completed easily in a short time. If the function source code changes, updating the performance profile is required for the modified function, which is comparatively timeconsuming and perhaps costly.



Fig. 8. Workflow of serverless applications used in the experimental evaluation of performance and cost models. The number on each edge represents the transition probability. The workflow of App16 is as shown. The workflow of other four Apps can be obtained by removing and replacing all edges and functions in corresponding box(es) with an edge whose transition probability is 1. The transition delay is defined using the delay model of AWS Step Functions. The applications are composed of functions with three different types of workload depicted by three colors.

#### **5** EXPERIMENTAL EVALUATION

We implement the performance and cost models and the PRCP algorithm using Python 3.8, and develop a ready-touse script to help developers make use of them. We validate the performance and cost model by conducting experiments on six serverless applications deployed on AWS, and examine the performance of the PRCP algorithm using an application with six functions. All algorithms, scripts, and experimental results are available in the artifact repository.

#### 5.1 Performance and Cost Models

#### 5.1.1 Experimental Design

To evaluate performance and cost models, we design five serverless applications composed of various number of FaaS functions with mixed types of workload. We deploy functions on AWS Lambda and employ AWS Step Functions as the serverless application coordinator. AWS Step Functions is a serverless workflow coordination service that combines multiple Lambda functions and other serverless services offered by AWS into responsive serverless applications [20].

We design FaaS functions with three different types of workload, namely CPU intensive, disk I/O intensive, and network I/O intensive. The CPU-intensive workloads include string hashing, floating-point arithmetic, and recursive calculation. The disk-intensive workload is to write and read several files to the hard disk drive. The networkintensive workload is designed to download and upload a number of files from and to the AWS S3 bucket. We develop sixteen functions with different input sizes and types of workload and host them on AWS Lambda.

By leveraging AWS Step Functions, we develop five serverless applications using those sixteen functions, which are App8, App10, App12, App14, and App16. The numeric suffix of the application name represents the number of functions in the application. From App8 to App16, we increase the number of functions from eight to sixteen, as well as the number of structures (parallels, branches, cycles, and self-loops) in the application workflow. As a result, the complexity of the workflow grows accordingly. Besides, each application has a combination of all three types of workloads, making them truly representative of actual serverless applications on cloud. The workflow of five serverless applications are shown together in Figure 8.

We deploy sixteen functions on AWS Lambda and obtain their average duration under a feasible memory configuration by invoking each of them 720 times. Five aforementioned serverless applications are developed and deployed on AWS Step Functions. For repeatability and rigorousness, we follow the methodological principles proposed by Papadopoulos et al. [39] and execute repeated experiments and long runs. We execute each application for five periods of two hours with a two-hour interval between two consequent periods. During each period, each application is executed continuously with a 10-second interval between two consequent invocations. For each execution period, we discard executions in the first and last 10 minutes to avoid any transient fluctuations in performance and only adopt invocations between them. By doing so, for each application, logs of 3,000 invocations are ready for analysis.

#### 5.1.2 Experimental Result

By giving the workflows and the average duration and allocated memory size of functions as inputs, we leverage the proposed performance and cost models to obtain the average end-to-end response time and cost of five serverless applications. By analyzing logs of 3,000 invocations for each application, we compare the results of performance and cost models with the duration and billing logs reported by AWS.

Figure 9 and Figure 10 illustrate the experimental evaluation result of the performance and cost models. As is evident from the figures, both the average end-to-end response time and cost derived by the proposed performance and cost models are very close to the real values reported by AWS. Regardless of the complexity of the workflow, the accuracy of predicted average end-to-end response time and cost is over 97.5%. Such results indicate the high accuracy of the proposed performance and cost models.

#### 5.2 Performance and Cost Optimization

#### 5.2.1 Experimental Design

To evaluate the proposed performance and cost optimization solution, namely the PRCP algorithm, we develop a serverless application named App6. As the name suggests, App6 is composed of 6 functions with three types of workload (CPU-intensive, disk-intensive, network-intensive). For



Fig. 9. Experimental evaluation result of the performance model. As the number of functions in the application increases from 8 to 16, the workflow become more complex in terms of structures. The average accuracy is 98.75%. The box plot shows the maximal value, 25%, 50%, 75% percentiles and the minimal value of RT. The notch shows the 95% confidence interval for the median of RT.



Fig. 10. Experimental evaluation result of the cost model. The average accuracy is 99.97%.

generality, App6 is designed to have all 4 types of structures, namely the parallel, branch, cycle, and self-loop.

As described in Section 4.1, to optimize the performance and cost of the serverless application, a performance profiling phase is required to get the feasible memory configuration MOpt and performance profile PF of serverless functions in the application. We deploy functions on AWS Lambda, which allows the allocated memory to vary between 128 MB and 3,008 MB in 64MB increments, resulting in 46 possible choices. We stipulate that all 46 memory sizes are feasible choices for all functions. For each function, we obtain its performance profile by the performance profiling phase, during which the function is invoked 100 times under each feasible memory size, and the duration is logged.

In order to measure the accuracy of solutions given by the PRCP algorithm, an exhaustive search is necessary to obtain the performance and cost of App6 under all possible memory configurations. However, 6 functions with 46 possible memory choices lead to 9.47 billion states, making the exhaustive search computationally unfeasible. Therefore, we trim the number of memory choices while retain the trend of the response time-memory size curve by sampling the performance profile. After sampling, the viable memory size of each function varies between 128 MB and 3,008 MB



Fig. 11. The workflow of App6. The legend is same as Figure 8.

in 192 MB increments, 16 choices left. Using the proposed performance and cost models, we exhaustively obtain the average end-to-end response time and cost of App6 under 16,777,216 different memory configurations. As evidenced in Section 5.1.2, the performance and cost models can accurately give the average end-to-end response time and cost of the serverless application. Therefore, despite the fact that we do not perform the test on AWS Step Functions to get the performance and cost of App6 under 16,777,216 configurations, which is financially and practically unfeasible, the average end-to-end response time and cost derived from proposed models can be regarded as actual values.

We choose the series of 100 equidistant values between the minimum cost and the maximum cost as the budget constraints and execute the PRCP algorithm to solve the BPBC problem with four types of greedy strategies. Similarly, we use the series of 100 equidistant values between the minimum and the maximum end-to-end response time as the performance constraints and solve the BCPC problem. We compare the best performance and the best cost given by the PRCP algorithm with the actual value derived by the exhaustive search under each constraint value.

#### 5.2.2 Experimental Result

Figure 11 shows the workflow of App6, and the performance profile of functions is illustrated as Figure 12. There are 1 parallel, 1 branch, 1 cycle, and 1 self-loop in App6.

Figure 13 depicts the best performance for the BPBC problem achieved by the PRCP algorithm with four greedy strategies. Considering the best performance among solutions given by four strategies, compared to the ideal value, the accuracy of the algorithm is calculated. For the 100 budget constraints, the average accuracy of the PRCP algorithm is 97.40%. Figure 14 illustrates the best cost achieved by the PRCP algorithm solving the BCPC problem. For the 100 performance constraints, the average accuracy of the PRCP algorithm is 99.63%. As is evident from Figure 13 and Figure 14, the accuracy of different greedy strategies varies with different budget and performance constraints. Therefore, the best method is to employ all four greedy strategies in the PRCP algorithm and select the best solution that is closest to the target performance or cost constraint.

#### 6 RELATED WORK

The serverless computing paradigm has attracted a great deal of interest from both academia and industry [8], [19], [40]. However, few research studies have been directed at the modeling and optimization of performance and cost of serverless applications. Therefore, we provide an extensive review of the literature in three fields, which are inherently related to our topic, namely the performance modeling of cloud applications, workflow scheduling in the cloud environment, and serverless architecture.



Fig. 12. The performance profile of 6 functions in App6. The allocated memory size varies between 128 MB and 3,008 MB in 64MB increments, resulting in 46 feasible memory choices.



Fig. 13. The result of the PRCP algorithm solving the BPBC problem. BCR threshold is 0.2. The budget constraints are 100 equidistant values between \$58.86 (minimum cost) and \$163.90 (maximum cost). The average accuracy of the best answer is 97.40%. The best answer is the minimal average response time among solutions.



Fig. 14. The result of the PRCP algorithm solving the BCPC problem. BCR threshold is 0.2. The performance constraints are 100 equidistant values between 2748.24 ms (minimum ERT) and 25433.08 ms (maximum ERT). The average accuracy of the best answer is 99.63%. The best answer is the minimal average cost among solutions.

#### 6.1 Performance models for cloud computing

The problem of modeling the performance of cloud architectures and applications has been extensively investigated over the past decade. Quality of service (QoS) requirements including response time, availability, and reliability, as well as monetary cost are the main focus of such models.

The queuing theory has been used to predict such QoS metrics for cloud systems. Khazaei et al. [41] obtained the

distribution of response time and blocking probability with regards to the number of servers and buffer size for a cloud center using a semi-Markov M/G/m/m + r queue, where r is the buffer size for incoming job. Using the task blocking probability and mean response delay as indicators, this work has been extended to predict the availability of cloud systems later [42]. Vilaplana et al. [43] utilized M/M/1 and M/M/m queues to model a single entry server and processing nodes on cloud to get the total response time with regards to the service rate of processing nodes.

Petri net has also been proven to be an effective formalism for modeling distributed systems with the concurrency and synchronization. Chen et al. [25] leveraged a deterministic and stochastic Petri net to illustrate the performance of producer/consumer based application models in the cloud environment. Cao et al. [26] developed an evaluation model based on Queuing Petri Net to model the throughput of cloud systems with three different architectures. Rista et al. [27] introduced the generalized stochastic Petri net model, composed of the combination of timed and nontimed nets, to predict the throughput and latency of the network in container-based cloud environments.

All these works either assumed the cloud system is designed homogeneously or required the parameters relevant to the underlying resources and incoming requests, which are not reasonable enough for the serverless paradigm because of the infrastructure-agnostic platform, event-driven and highly decoupled software architecture, auto-scaling resources, and elimination of resources management. Besides, these approaches focused more on the performance analysis and did not model the cost. We fill these gaps by proposing a definition of the serverless workflow, and to the best of our knowledge, the first performance and cost models that are compatible with the current serverless paradigm.

#### 6.2 Workflow scheduling in the cloud environment

In the past decade, researchers have extensively studied the workflow scheduling problem for workflow-based applications in the cloud environment. Abrishami et al. [37] presented a Partial Critical Paths algorithm to solve the best cost under the performance constraint problem for QoSbased workflows on the utility grid. Later, they extended the work by considering several cloud features such as the payas-you-go and duration-based billing model and applied the algorithm to a workflow instance on IaaS clouds to solve the same problem [38]. Lin et al. [33] proposed a Critical-Greedy algorithm to solve the best performance under the budget constraint problem for scientific applications. Faragardi et al. [44] proposed a Greedy Resource Provisioning with the consideration of heterogeneous cloud resources and the efficiency rate of instances to solve the best performance under the budget constraint problem for workflow applications on IaaS Clouds. Bao et al. [34] designed a Greedy Recursive Critical Path algorithm to find the configuration that achieves the best performance under the budget constraint for microservice-based applications on cloud.

This paper differs from the previous work at least in the following aspects: 1) We consider the new features in the serverless computing paradigm such as the memorydependent performance rules, GB-second billing model, independently operated components, and event-driven architecture. 2) The serverless workflow is not confined to DAGs, and cycles and self-loops are allowed to appear in the workflow. 3) We propose a Probability Refined Critical Path Algorithm to solve both BPBC and BCPC problems for serverless workflow based applications.

#### 6.3 Serverless architecture

Many cloud service providers have launched their FaaS platform, including AWS Lambda, Google Cloud Functions, and Microsoft Azure Functions in recent years. Since then, serverless computing has become an emerging technique and research topic in both industry and academia. There have been efforts made to topics including developing new applications [45], [46], migrating to serverless [47], and designing new software engineering methodology [48].

There have been some works on the performance profiling of FaaS platforms. Jackson et al. [49] investigated the impact of programming languages on the duration and cost of FaaS functions. Wang et al. [14] evaluated the performance of functions hosted on three FaaS platforms, which increases with the allocated memory size. They also observed that the underlying infrastructure of platforms is heterogeneous and overhead caused by cold starts. Figiela et al. [15] conducted performance tests by deploying a serverless workflow on four FaaS platforms and measured the data transfer delay between components and the container lifespan.

Several works presented a set of key challenges for the serverless architecture. The challenge that many studies have mentioned is the unpredictable performance and cost due to the lack of performance and cost models [6], [7], [8], [19]. The literate available on solving such a challenge is, however, very limited. Cold start latency and high communication overhead between components are also common concerns. Jonas et al. [19] discussed inadequate storage, high communication overhead, high cold start latency, and lack of predictable performance and cost of applications. Shahrad et al. [50] found the containerization incurs huge overhead and cold start brings the latency as high as 10 times of a small function's execution time. Hellerstein et al. [51] investigated cold start, limited storage, and communication overhead by case studies in distributed computing.

In this paper, we solve the unpredictable performance and cost problem for serverless applications with performance and cost models. We propose a serverless workflow with the consideration of the communication latency, and the cold start latency can be reflected in the model in a plugand-play manner. We also develop a heuristic algorithm to solve the performance-cost trade-off problem.

#### 7 CONCLUSION

In this work, we answered two research questions regarding the modeling and optimization of performance and cost of serverless applications. We laid out a formal definition of the serverless workflow with the consideration of several serverless features on clouds. Then we solved the unpredictable performance and cost problems for serverless applications by proposing the performance and cost models. The proposed models could accurately estimate the average endto-end response time and cost of serverless applications;

we checked the validity of the proposed models by extensive evaluation of five serverless applications deployed on Amazon AWS. Also, we solved two optimization problems, namely the best performance under the budget constraint and the best cost under the performance constraint. We answered them by proposing a heuristic algorithm named Probability Refined Critical Path algorithm with four greedy strategies. Again, we verified the validity of the proposed algorithms through experimental evaluations on AWS.

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